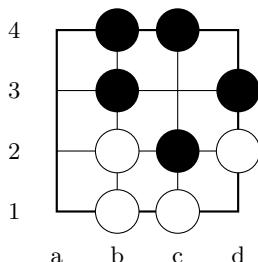


1. [5 points] Consider the following  $4 \times 4$  Go position after 7 moves, with White stones at b1, b2, c1, d2 and Black stones at b3, b4, c2, c4, d3.



- (a) List the liberties for the block containing c4. **a4, d4, a3, c3**
- (b) List the liberties for the block containing c2. **c3**
- (c) Suppose that White places a stone at c3. What stones, if any, does it capture? **c2**
- (d) Would it be legal for Black to reply by playing a stone at c2. Why or why not? **No, this move is forbidden by superko. (Also forbidden by basic ko, any answer referencing ko is acceptable)**
- (e) Would it be legal for Black to reply at d1 instead? Why or why not? **No, this move would be suicide. The stone at d2 has two liberties after White's capture of c2, so Black's move on d1 would not capture any stones, and would not have any liberties.**

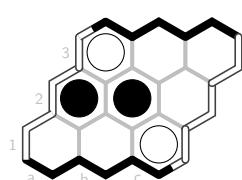
2. [5 points] The following line is from the go board initialization in `hexgo/stone_board.py`:

```
self.nbr_offset = ((-1,0),(0,1),(1,0),(0,-1))
```

- (a) Explain the purpose of this line. **These are the coordinate offsets of every possible neighbouring point; adding each of these tuples elementwise to the row-column coordinates of a point will give coordinates which, if they are in range, will be the coordinates of a neighbouring point.**
- (b) Give the corresponding line for Hex board initialization with neighbour order below left, below right, right, above right, above left, left. **Full marks for any of**

```
self.nbr_offset = ((-1,0),(-1,1),(0,1),(1,0),(1,-1),(0,-1)) or
self.nbr_offset = ((1,0),(1,1),(0,1),(-1,0),(-1,-1),(0,-1)) or
self.nbr_offset = ((-1,-1),(-1,0),(0,1),(1,1),(1,0),(0,-1)) or
self.nbr_offset = ((1,-1),(1,0),(0,1),(-1,1),(-1,0),(0,-1))
```

**(because lectures and example code are inconsistent about whether we count down from the top row or up from the bottom row, and because it's fine for above left to be in the same column and below left to be over one, or for above left to be over one and below left to be in the same column.)**
**Half marks if all the elements are correct but the order is wrong.**
- 3. [5 points] Here are the `parent[x]` values after the position below has been created by the moves 1.B[a2], 2.W[a3], 3.B[b2], 4.W[c1]. Next, a black stone is played at a1. Recall that `Union(p,q)` sets the parent of the root of q's component to the root of p's component; assume *no* union-by-rank optimization. Below, show the new values of `parent[x]` after each union. TP,BM,LF,RT are the top, bottom, left, right borders respectively.



x	TP	BM	LF	RT	a1	b1	c1	a2	b2	c2	a3	b3	c3
current parent[x]	TP	BM	LF	RT	a1	b1	RT	a2	a2	c2	LF	b3	c3
after Union(a2,a1)	TP	BM	LF	RT	a2	b1	RT	a2	a2	c2	LF	b3	c3
then after Union(BM,a1)	TP	BM	LF	RT	a2	b1	RT	BM	a2	c2	LF	b3	c3

4. [5 points] Here is a portion of the `tromp_taylor_score` method in `go/go_helper.py`, with two lines missing. The method counts White territory into the variable `wt` and Black territory into the variable `bt`.

```
1  while (len(empty_points) > 0):  
2      q = empty_points.pop()  
3      for j in self.nbr_offsets:  
4          x = j + q  
5          b_nbr |= (self.brd[x] == BLACK)  
6          w_nbr |= (self.brd[x] == WHITE)  
7          if (self.brd[x] == EMPTY and  
8              x not in empty_seen):  
9              empty_seen.add(x)  
10             empty_points.append(x)  
11             territory += 1  
12             if b_nbr and not w_nbr:  
13                 -----line_(A)-----  
14             elif w_nbr and not b_nbr:  
15                 -----line_(B)-----
```

(a) What should lines (A) and (B) be?

Line A should be `bt += territory` and  
Line B should be `wt += territory`.

(b) Explain the purpose of line 6.

Line 6 sets `w_nbr` to True when a White stone is encountered and never sets it back to False; after the while loop completes it will be True iff `q` reaches any White stone.