# Neural Networks for Sequence Data

CMPUT 261: Introduction to Artificial Intelligence

GBC §10.0-10.2 P §12.1-12.2, 12.4-12.5

#### Lecture Outline

- 1. Midterm Review
- 2. Recap & Logistics
- 3. Unfolding Computations
- 4. Recurrent Neural Networks
- 5. Attention & Transformers

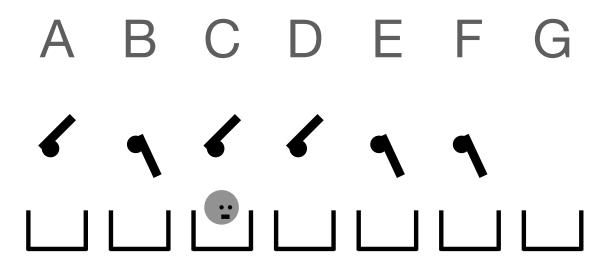
After this lecture, you should be able to:

- demonstrate unfolding a recurrent expression
- explain the problems with handling sequence input using dense or convolutional neural networks
- explain the high-level idea behind neural networks and transformers
- describe how self-attention combines inputs to generate its outputs
- describe the architecture of a transformer layer
- explain the high-level idea behind encoder-decoder architectures

(b) [2 points] How many states does this search problem have?

You need to track the states of all the switches

#### Midterm Review: Admissible Heuristic

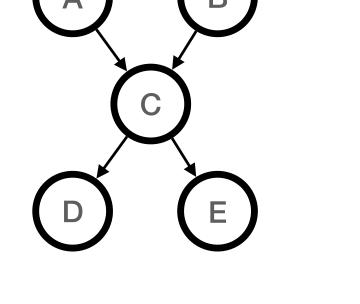


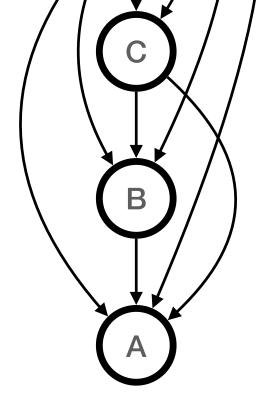
Consider the following heuristic function:

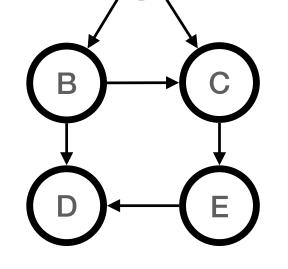
$$h(s) = \sum_{\text{positions } y} 1[\text{switch at position } y \text{ is off}] d(\text{pos}(s), y).$$

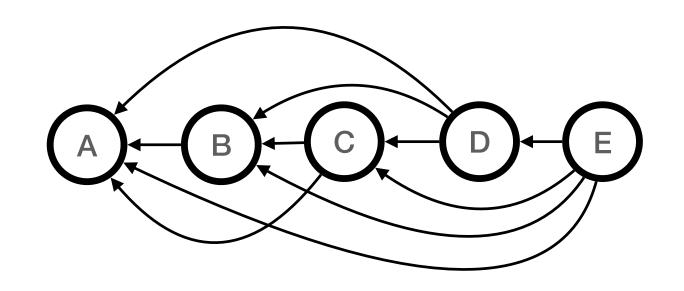
Is the heuristic function h an  $admissible\ heuristic$  for this problem? Why or why not?

- ullet Heuristic adds up cost to get from current position to position y for every position y
- But that's more actions than you need to take for any solution
- Question: What will h return from a state where all the switches are in the off state and SwitchBot is in position  $\mathbf{G}$ ?
- Question: Can an admissible heuristic ever dominate a non-admissible heuristic?

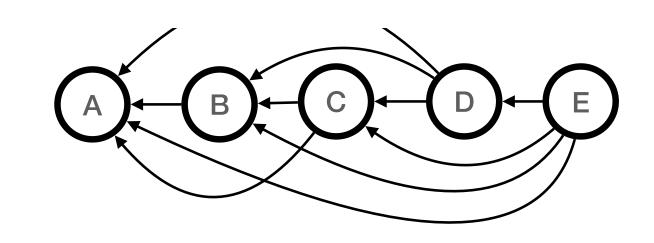






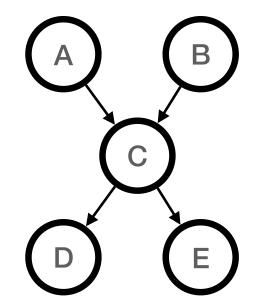


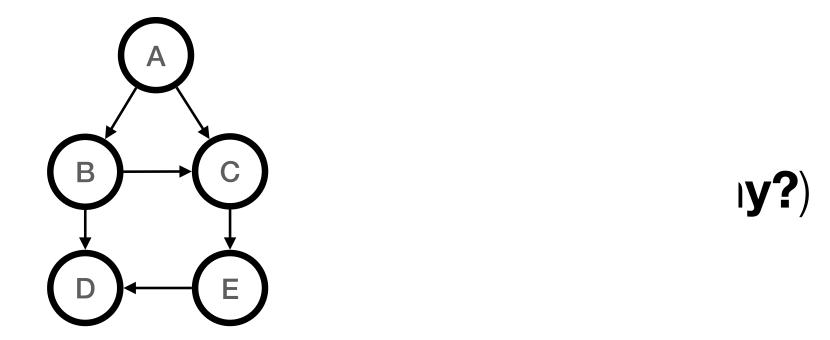
 $P(A)P(B \mid A)P(C \mid A, B)P(D \mid B, E)P(E \mid C)$ 





C D E



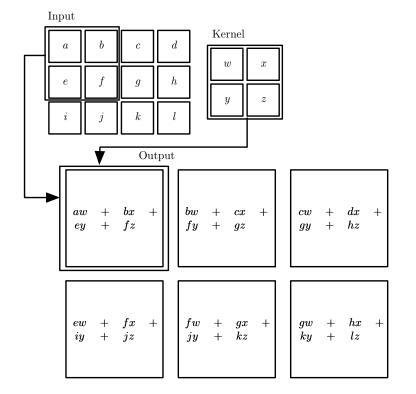


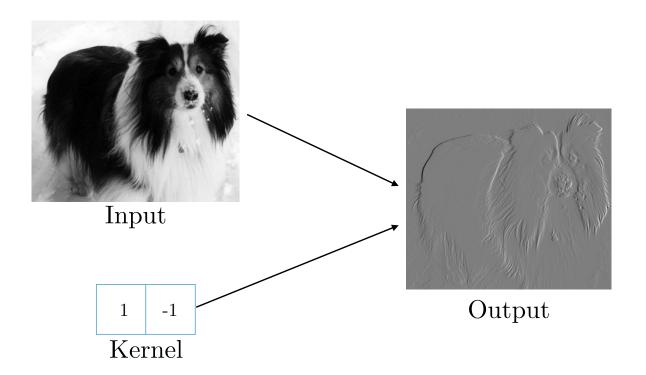
# Logistics: Assignment #3

- Assignment 3 is due Thursday (Mar 23) at 11:59pm
  - Late submissions until the following Monday with 20% deduction

# Recap: Convolutional Neural Networks

- Convolutional networks: Specialized architecture for images
- Number of parameters controlled by using convolutions and pooling operations instead of dense connections
- Fewer parameters means more efficient to train





(Images: Goodfellow 2016)

# Sequence Modelling

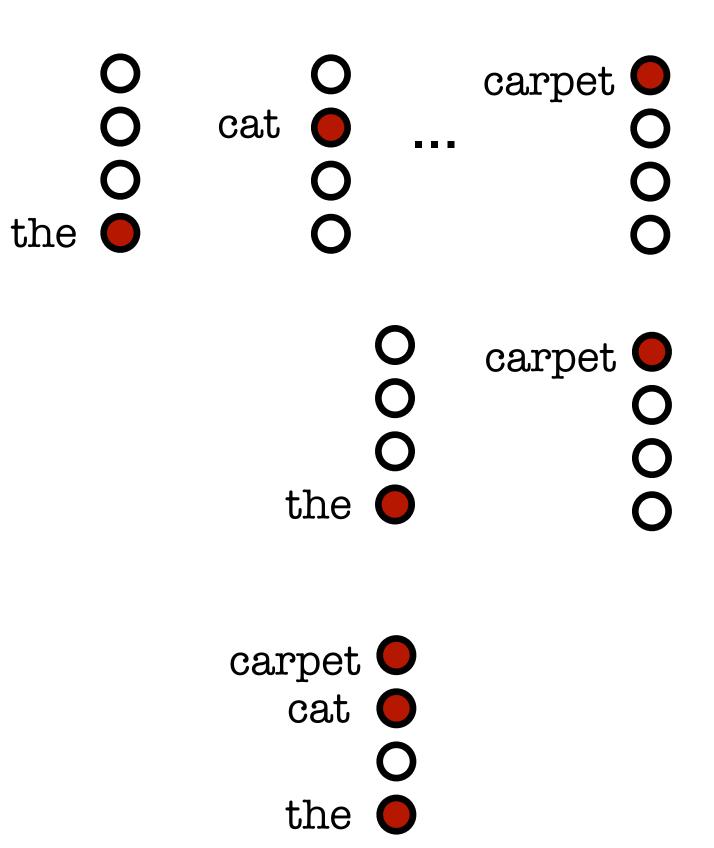
- For many tasks, especially involving language, we want to model the behaviour of sequences
- **Example:** Translation
  - The cat is on the carpet  $\implies$  Le chat est sur le tapis
- Example: Sentiment analysis
  - This pie is great ⇒ POSITIVE
  - This pie is okay, not great ⇒ NEUTRAL
  - This pie is not okay  $\Rightarrow$  NEGATIVE

#### Sequential Inputs

The cat is on the carpet

**Question:** How should we **represent** sequential input to a neural network?

- 1. 1-hot vector for each word
   (Sequence must be a specific length?)
- 2. 1-hot vector for **last few words** (*n*-gram)
- 3. Single vector indicating each word that is present (bag of words)



# One-Hot Representations

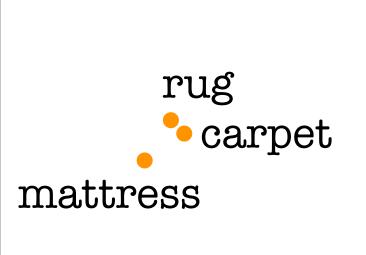
carpet

One-hot representations of words have some problems:

- 1. **Wasteful:** Each input vector must have a dimension equal to the size of the vocabulary (possible words)
  - If vocabulary has 30,000 words, then each vector has 29,999 zeros
- 2. Poor generalization: Ideally, similar words would be treated similarly
  - Exploiting meaningful similarity between images was an important feature of convolutional neural networks

# Semantic Embeddings

- The usual approach is to first learn a semantic embedding for one-hot vectors
- Every word gets represented as a dense vector with smaller dimension than the vocabulary (typical size: 1,024)
- Goal: Words with similar meanings will have small distance between embedded vectors; words with different meanings will have large distance between embedded vectors





#### (Pre-)Training Semantic Embeddings

**Question:** How many parameters are required to convert a one-hot encoding for vocabulary of V words into a D-dimensional embedding?

- Embeddings require the training of *many* parameters
- Fortunately, this can be done with unlabeled data
- **Trick:** "Pre-train" neural network for a task that we don't care about
  - But which can be evaluated using unlabeled data
  - Predicting words from k nearby words
  - Predicting "masked" words
- Keep the weights that convert the one-hot layer into a dense embedding layer
- Throw away the weights that convert the embedding layer into output

# Processing Variable-Length Sequences

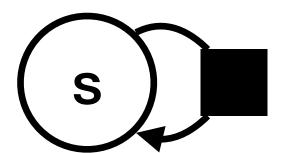
- Image inputs can be restricted to a standard size (20x20, 1024x768, etc.)
- Sequence inputs (e.g., text) are variable-length
  - And often very long
- Solution: Apply the same operations to each position in the sequence
- Two such approaches:
  - 1. **Recurrent neural networks:** input is current token + fixed-dimension "state" from previous operation
  - 2. **Transformers / self-attention:** Size of state varies with size of sequence

#### Dynamical Systems

• A dynamical system is a system whose state at time t+1 depends on its state at time t:

$$\mathbf{s}^{(t)} = f(\mathbf{s}^{(t-1)}; \theta)$$

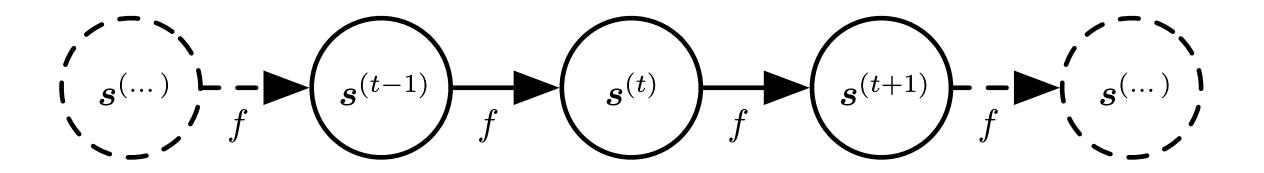
 An expression that depends on the same expression at an earlier time is recurrent.



### Unfolding Computations

 A recurrent expression can be converted to a non-recurrent expression by unfolding:

$$\mathbf{s}^{(3)} = f(\mathbf{s}^{(2)}; \theta)$$
$$= f(f(\mathbf{s}^{(1)}; \theta); \theta)$$

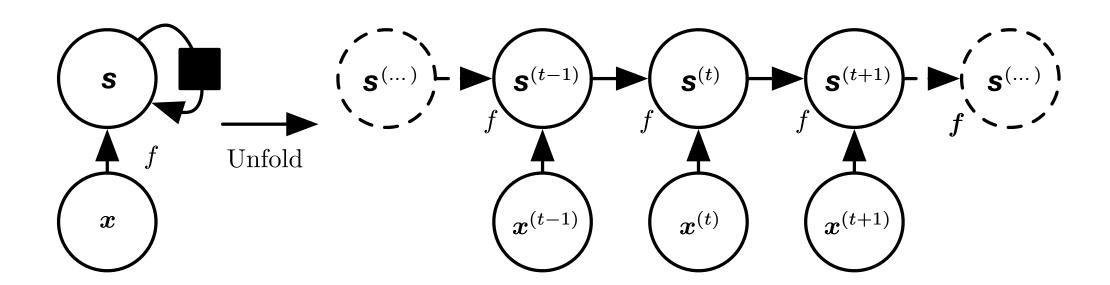


### External Signals

• Dynamical systems can also be driven by external signals:

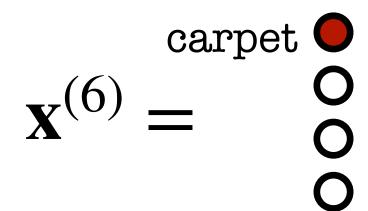
$$\mathbf{s}^{(t)} = f(\mathbf{s}^{(t-1)}, \mathbf{x}^{(t)}; \theta)$$

• These systems can also be represented by non-recurrent, unfolded computations:



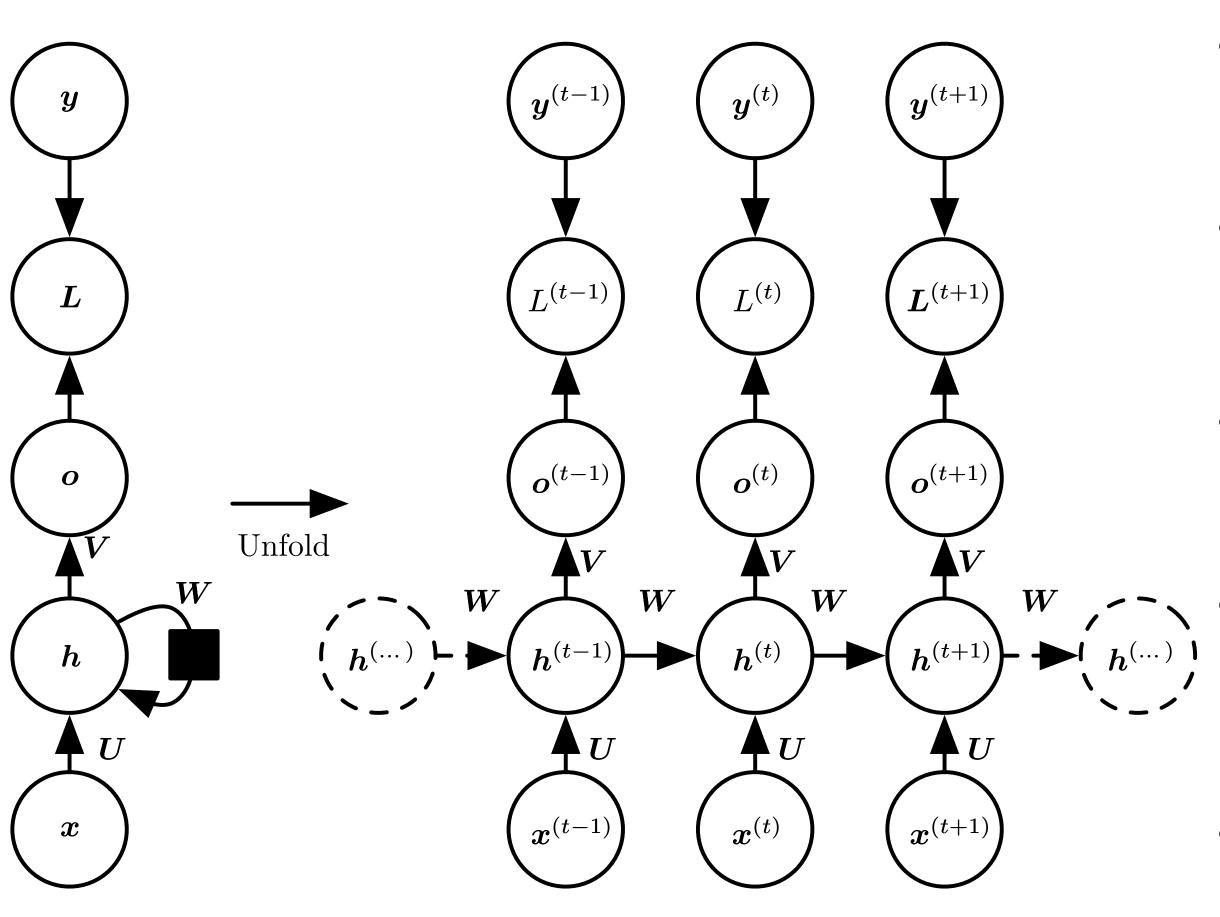
#### Recurrent Neural Networks

- Recurrent neural network: a specialized architecture for modelling sequential data
- Input presented one element at a time



- Parameter sharing by:
  - Treating the sequence as a system with state
  - Introducing hidden layers that represent state
  - Computing state transitions and output using same functions at each stage
- The same computation is applied to each pair of state and input
  - But the state is different after each application

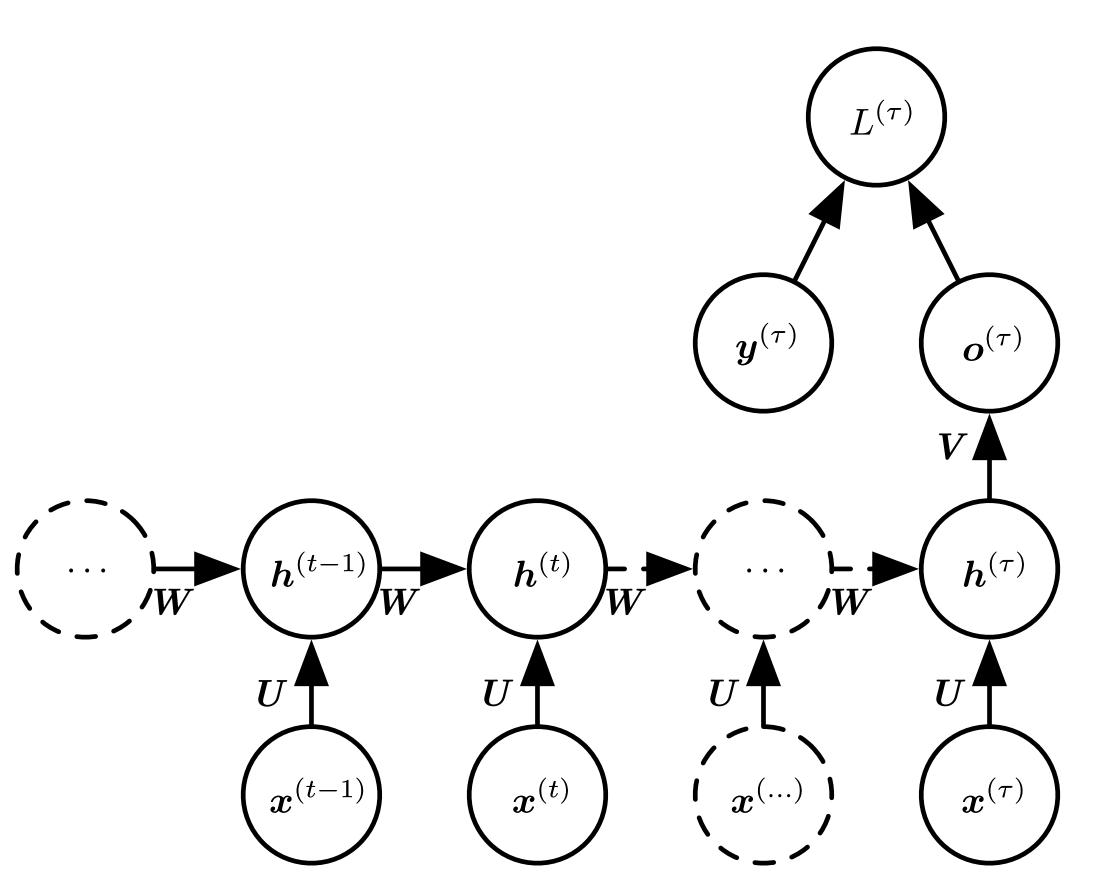
#### Recurrent Hidden Units: Sequence to Sequence



- Input values  $\boldsymbol{x}$  connected to hidden state  $\boldsymbol{h}$  by weights  $\boldsymbol{U}$
- Hidden state  ${f h}$  mapped to  ${f output}\ {f o}$  by weights  ${f V}$
- Hidden state  $\mathbf{h}^{(t-1)}$  connected to hidden state  $\mathbf{h}^{(t)}$  by weights  $\mathbf{W}$
- Gradients computed by back propagation through time: from final loss all the way back to initial input.
- All hidden states computed must be stored for computing gradients

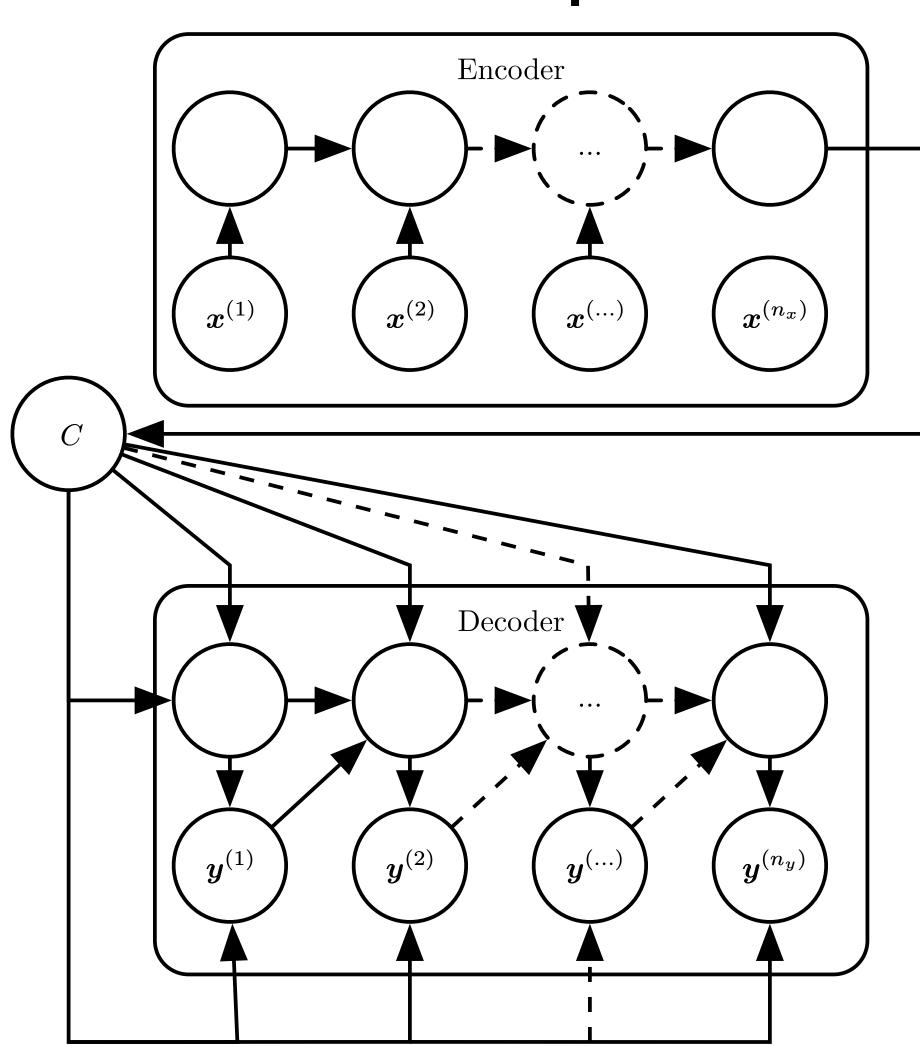
(Image: Goodfellow 2016)

### Recurrent Hidden Units: Sequence to Single Output



- Update state as inputs are provided
- Only compute a single output at the end
- W, U still shared at every stage
- Back propagation through time still requires evaluating every state in gradient computation

# Encoder/Decoder Architecture for Sequence to Sequence



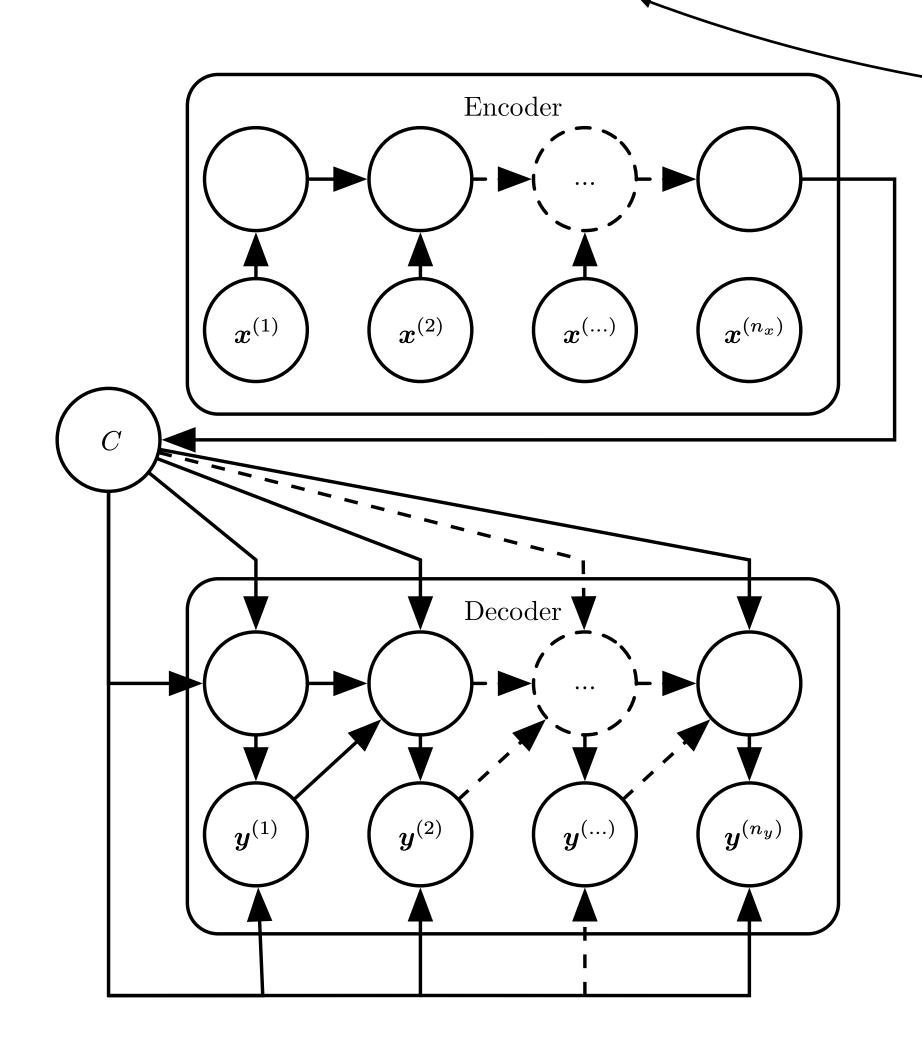
Can combine approaches for sequence-to-sequence:

- 1. Accept entire input to construct a single "context" output **C**
- 2. Construct new sequence using context **C** as **only input**

(Image: Goodfellow 2016)

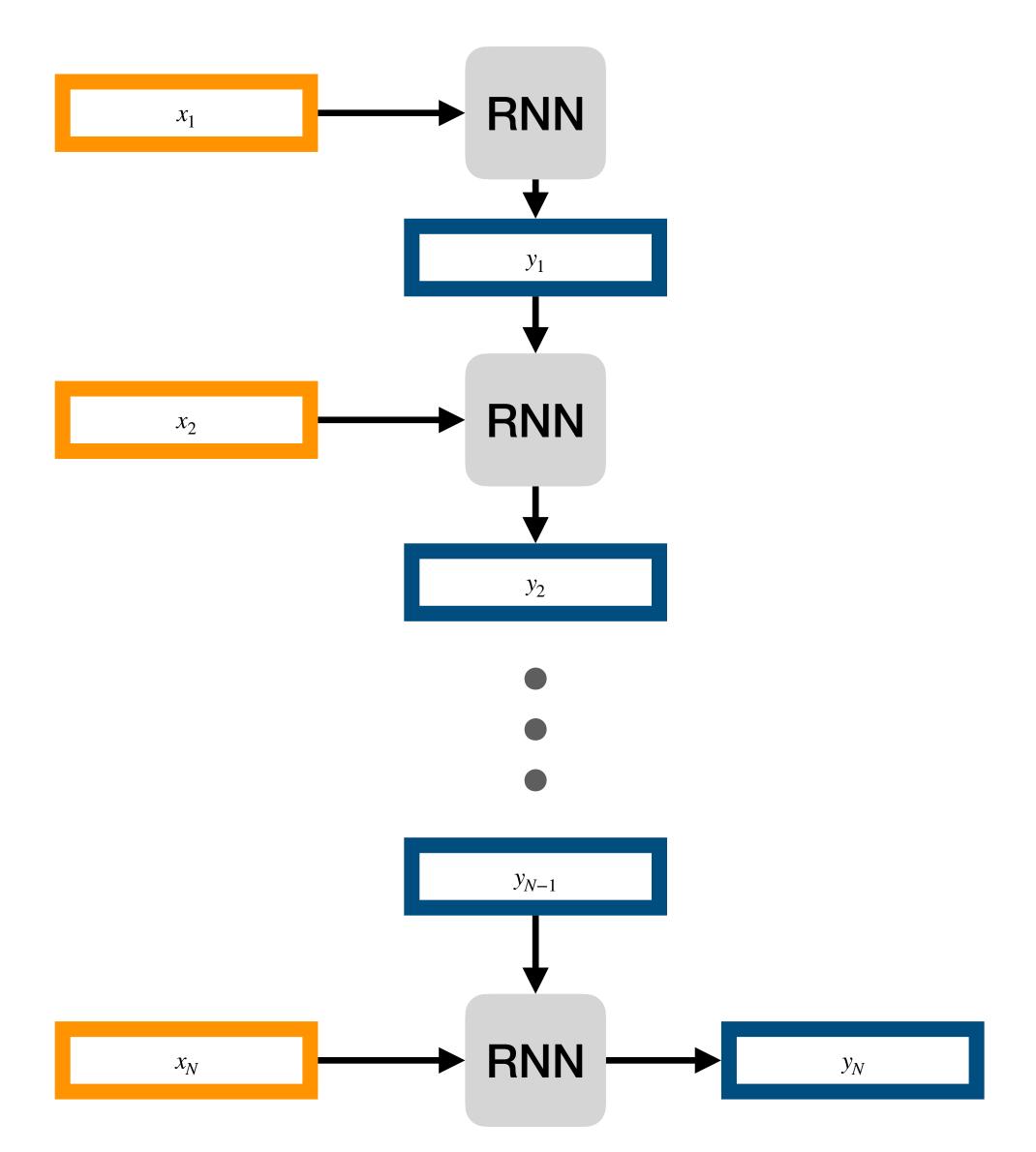
# Long-Range Dependence

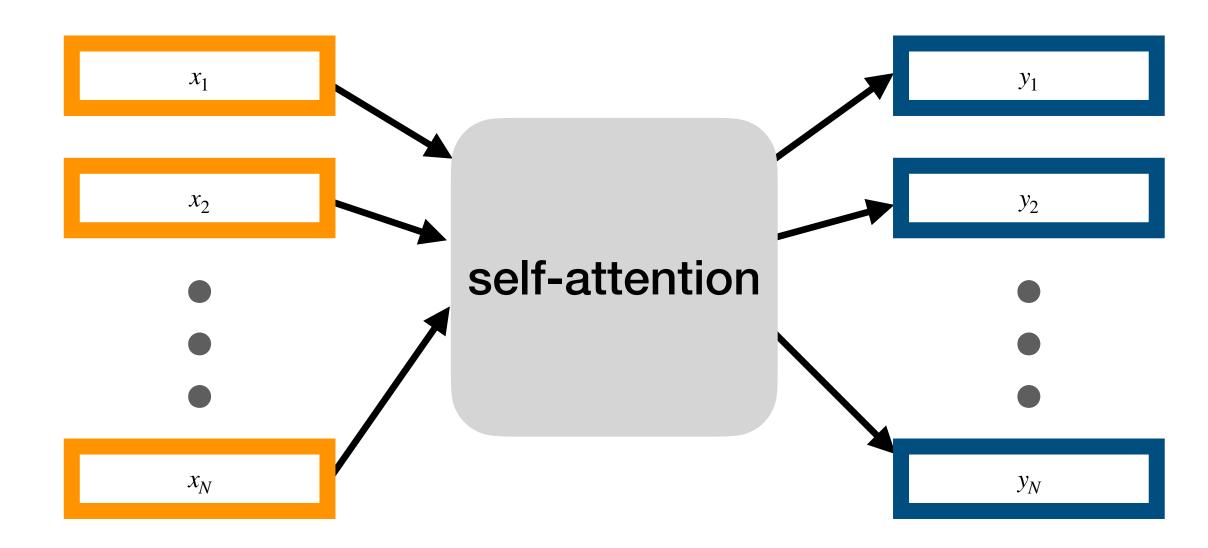
The submarine, which was the subject of a well known song by the Beatles, was yellow.



- Information sometimes needs to be accumulated for a long part of the sequence
- But how long an individual piece of information should be accumulated is context-dependent
- Long-range dependence can be difficult for a recurrent network
  - Often need to accumulate information in the state, and then forget it later

#### Self-Attention vs. RNN





- RNN: accept "previous" state and current input; output "next" state
  - Final output is last state
- Self-attention: Accept ALL inputs
  - Final output is ALL states

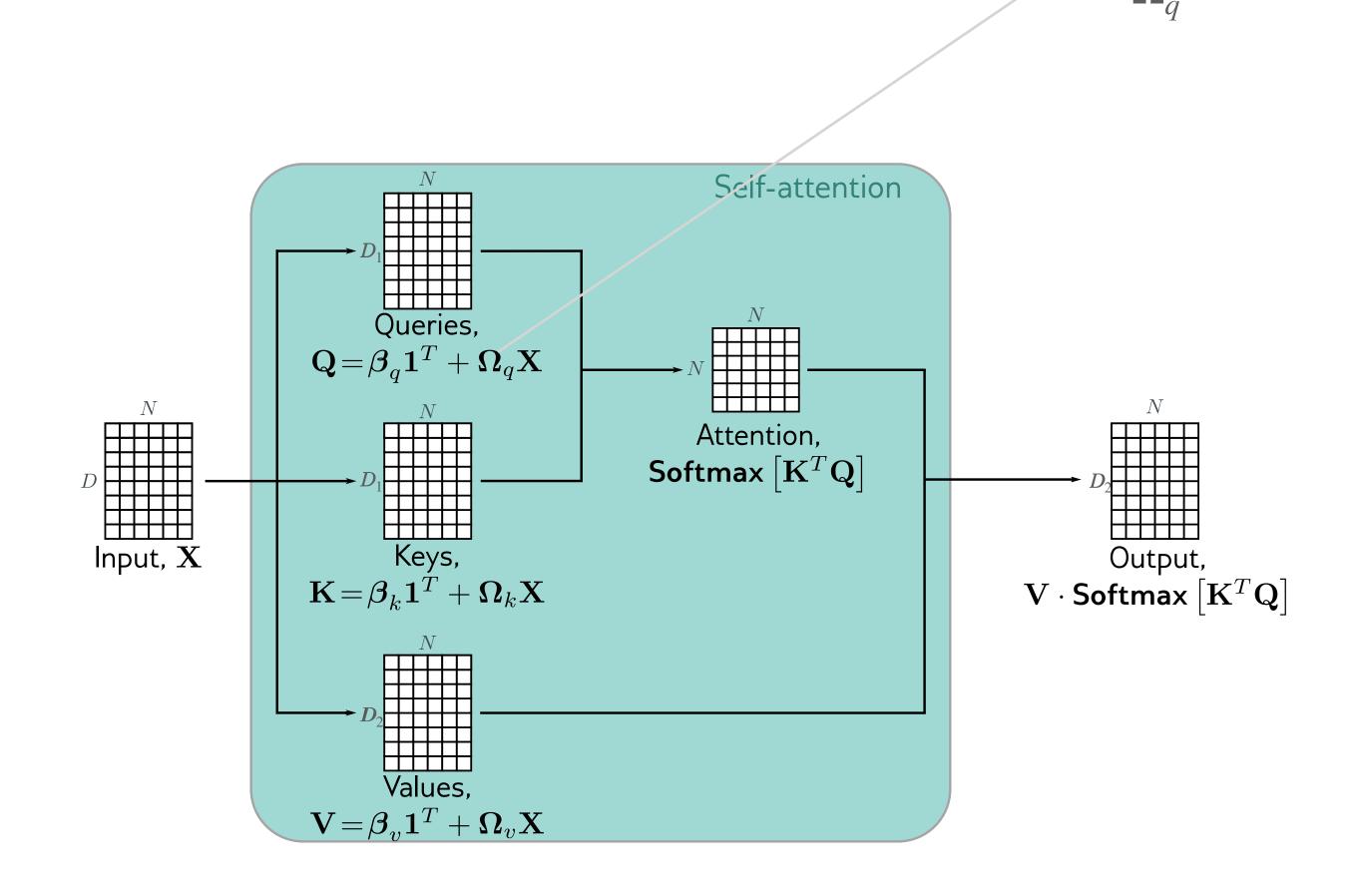
#### Self-Attention

- A self-attention unit computes three values for each input i:
  - Query  $q_i$ , Key  $k_i$ , and Value  $v_i$
  - These values are computed in the same way for each input
- Each output is a weighted combination of the values of all inputs:

$$y_j = \sum_i w_{ij} v_i$$

• Weight for output j of value i is the dot-product of j's query and i's key

$$w_{ij} = q_j^{\mathsf{T}} k_i$$



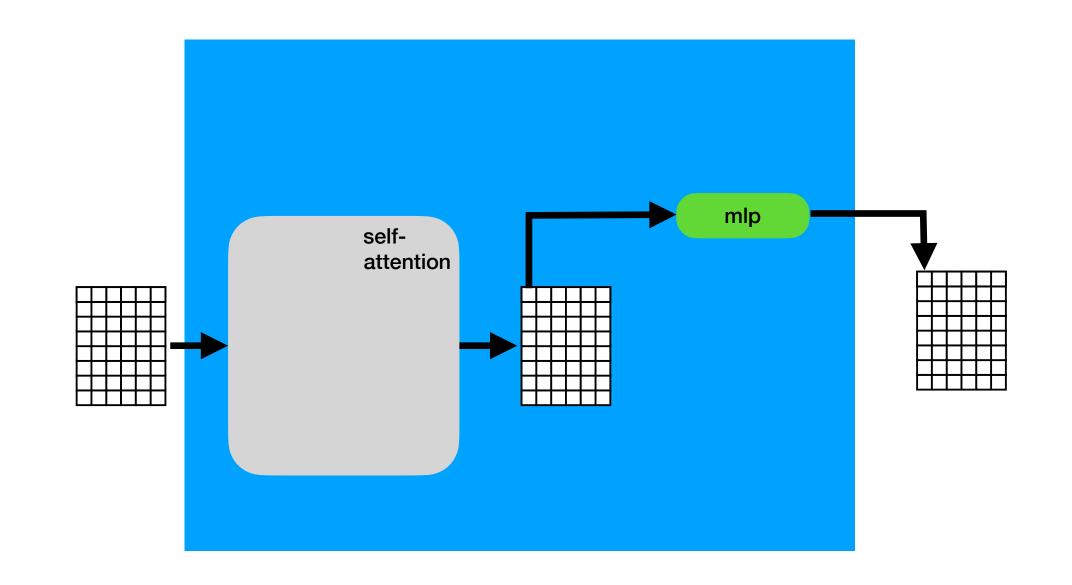
(Image: Prince 2022)

#### Transformer Blocks

- A transformer layer is a selfattention unit followed by a dense feedforward network
  - The **same** feedforward network gets applied to each output of the self-attention unit:

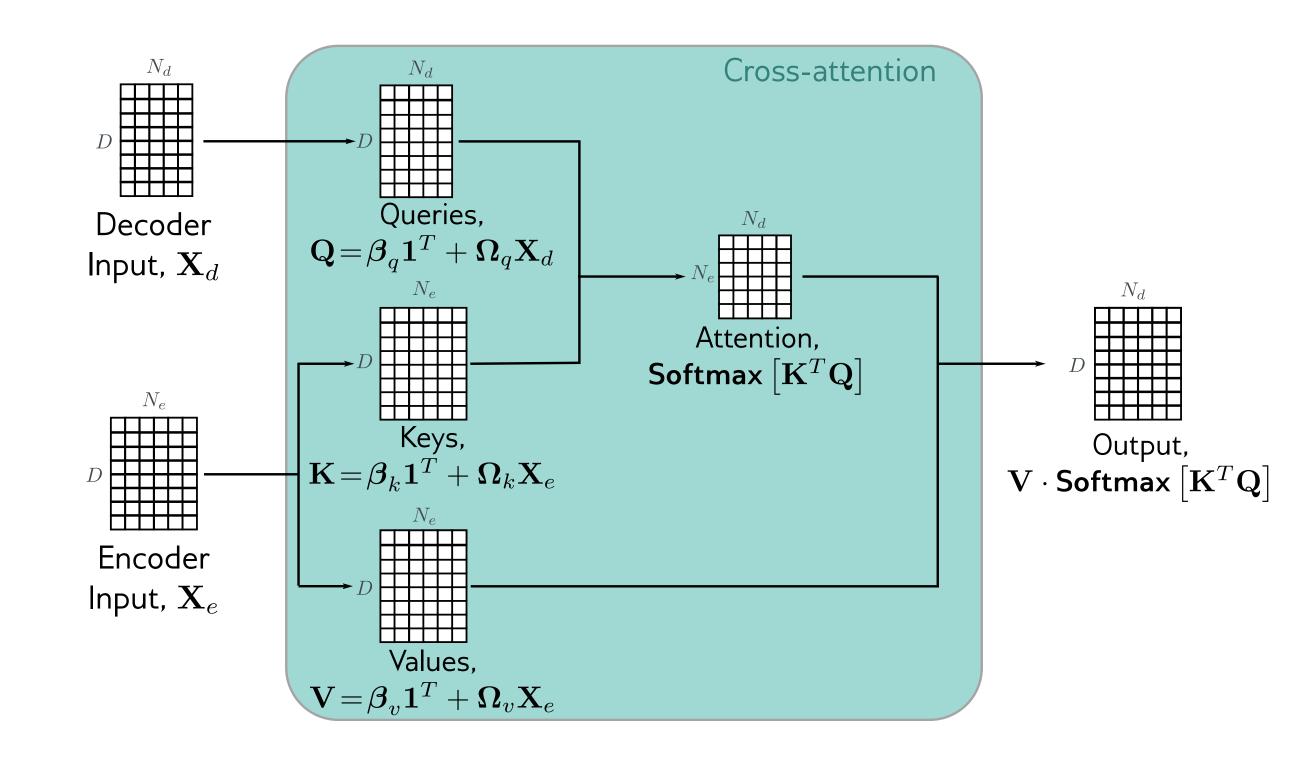
$$y_j = \text{mlp}(x_j; \Omega)$$
 for  $j = 1,...,N$ 

 In a typical transformer architecture, several transformer blocks will be strung together in parallel

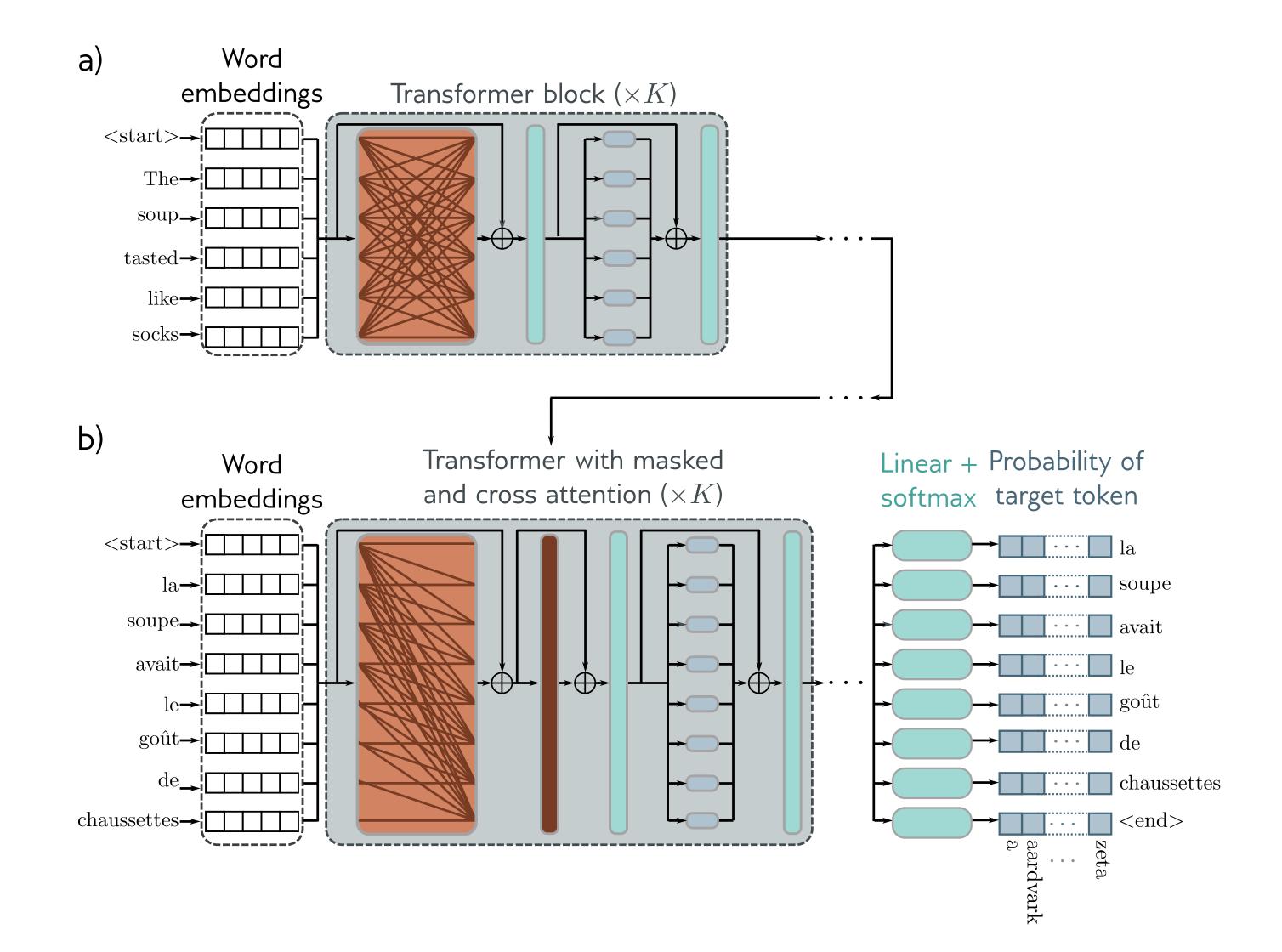


#### Cross-Attention

- The transformers described so far will construct a context: an encoding of the sequence
- For some tasks (e.g., translation), this encoding must then be decoded
- Decoder looks almost identical to encoder, except that it attends to the context as well as the previous input
- This is accomplished using cross-attention



#### Example Encoder-Decoder



(Image: Prince 2022)

# Summary

- Naïvely representing sequential inputs for a neural network requires infeasibly many input nodes (and hence parameters)
- One-hot encodings are wastefully large and have no semantic structure
  - Embeddings solve these problems and can be trained without explicit labels
- Recurrent neural networks are a specialized architecture for sequential inputs
  - State accumulates across input elements
  - Each stage computed from previous stage using same parameters
- Transformers are another specialized architecture!
  - Self-attention to combine inputs instead of accumulating state
  - All states output (not just last in a sequence)
  - Improved ability to attend to long-range dependence
  - Admits of better parallel evaluation