Temporal Difference Learning

CMPUT 366: Intelligent Systems

S&B §6.0-6.2, §6.4-6.5

Labs & Assignment #3

- Assignment #3 was due Mar 25 (today) before lecture
- Today's lab is from 5:00pm to 7:50pm in CAB 235
 - Last-chance lab for late assignments
 - Not mandatory
 - Opportunity to get help from the TAs

Lecture Overview

- 1. Recap
- 2. TD Prediction
- 3. On-Policy TD Control (Sarsa)
- 4. Off-Policy TD Control (Q-Learning)

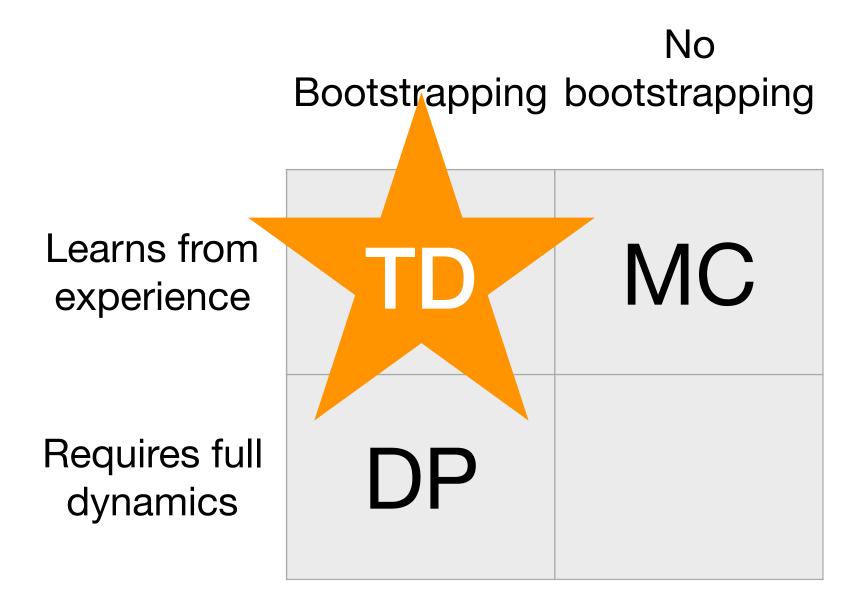
Recap: Monte Carlo RL

- Monte Carlo estimation: Estimate expected returns to a state or action by averaging actual returns over sampled trajectories
- Estimating action values requires either exploring starts or a soft policy (e.g., ε-greedy)
- Off-policy learning is the estimation of value functions for a target policy based on episodes generated by a different behaviour policy
- Off-policy control is learning the optimal policy (target policy)
 using episodes from a behaviour policy

Learning from Experience

- Suppose we are playing a blackjack-like game in person, but we don't know the rules.
 - We know the actions we can take, we can see the cards, and we get told when we win or lose
- Question: Could we compute an optimal policy using dynamic programming in this scenario?
- Question: Could we compute an optimal policy using Monte Carlo?
 - What would be the pros and cons of running Monte Carlo?

Bootstrapping



- Dynamic programming bootstraps: Each iteration's estimates are based partly on estimates from previous iterations
- Each Monte Carlo estimate is based only on actual returns

Updates

- Dynamic Programming: $V(S_t) \leftarrow \sum_{a} \pi(a \mid S_t) \sum_{s',r} p(s',r \mid S_t,a) [r + \gamma V(s')]$
- Monte Carlo: $V(S_t) \leftarrow V(S_t) + \alpha \left[G_t V(S_t) \right]$

• TD(0): $V(S_t) \leftarrow V(S_t) + \alpha \left[R_{t+1} + \gamma V(S_{t+1}) - V(S_t) \right]$

$$v_{\pi}(s) \doteq \mathbb{E}_{\pi}[G_t \mid S_t = s]$$
 Monte Carlo: Approximate because of \mathbb{E}
$$= \mathbb{E}_{\pi}[R_{t+1} + \gamma G_{t+1} \mid S_t = s]$$

$$= \mathbb{E}_{\pi}[R_{t+1} + \gamma v_{\pi}(S_{t+1}) \mid S_t = s] \cdot \text{Dynamic programming:}$$
 Approximate because v_{π} not known

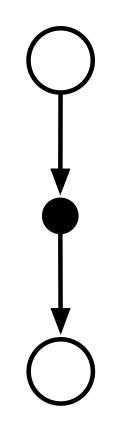
TD(0): Approximate because of \mathbb{E} and \mathbf{v}_{π} not known

TD(0) Algorithm

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Input: the policy \pi to be evaluated Algorithm parameter: step size \alpha \in (0,1] Initialize V(s), for all s \in \mathbb{S}^+, arbitrarily except that V(terminal) = 0 Loop for each episode:

Initialize S
Loop for each step of episode:

A \leftarrow \text{action given by } \pi \text{ for } S
Take action A, observe R, S'
V(S) \leftarrow V(S) + \alpha \left[R + \gamma V(S') - V(S)\right]
S \leftarrow S'
until S is terminal
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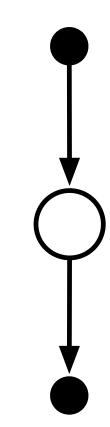
Question: What information does this algorithm use?

TD for Control

- We can plug TD prediction into the generalized policy iteration framework
- Monte Carlo control loop:
 - 1. Generate an episode using estimated π
 - 2. Update estimates of Q and π
- On-policy TD control loop:
 - 3. Take an **action** according to π
 - 4. Update estimates of Q and π

On-Policy TD Control

Sarsa (on-policy TD control) for estimating $Q \approx q_*$ Algorithm parameters: step size $\alpha \in (0,1]$, small $\varepsilon > 0$ Initialize Q(s,a), for all $s \in \mathcal{S}^+$, $a \in \mathcal{A}(s)$, arbitrarily except that $Q(terminal, \cdot) = 0$ Loop for each episode: Initialize SChoose A from S using policy derived from Q (e.g., ε -greedy) Loop for each step of episode: Take action A, observe R, S'Choose A' from S' using policy derived from Q (e.g., ε -greedy) $Q(S,A) \leftarrow Q(S,A) + \alpha \left[R + \gamma Q(S',A') - Q(S,A)\right]$ $S \leftarrow S'$; $A \leftarrow A'$;



Question: What information does this algorithm use?

until S is terminal

Question: Will this estimate the Q-values of the optimal policy?

Actual Q-Values vs. Optimal Q-Values

- Just as with on-policy Monte Carlo control, Sarsa does not converge to the optimal policy, because it always chooses an ε-greedy action
 - And the estimated Q-values are with respect to the actual actions, which are ε-greedy
- **Question:** Why is it necessary to choose ε -greedy actions?
- What if we acted ε -greedy, but learned the Q-values for the optimal policy?

Off-Policy TD Control

Q-learning (off-policy TD control) for estimating $\pi \approx \pi_*$

Algorithm parameters: step size $\alpha \in (0,1]$, small $\varepsilon > 0$ Initialize Q(s,a), for all $s \in S^+, a \in \mathcal{A}(s)$, arbitrarily except that $Q(terminal, \cdot) = 0$ Loop for each episode:

Initialize S

Loop for each step of episode:

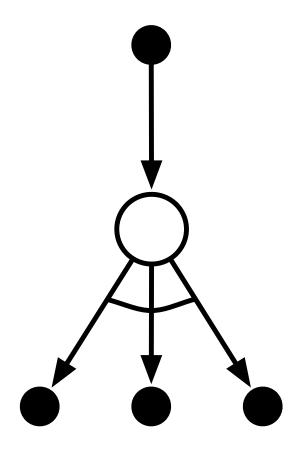
Choose A from S using policy derived from Q (e.g., ε -greedy)

Take action A, observe R, S'

$$Q(S,A) \leftarrow Q(S,A) + \alpha \left[R + \gamma \max_{a} Q(S',a) - Q(S,A) \right]$$

$$S \leftarrow S'$$

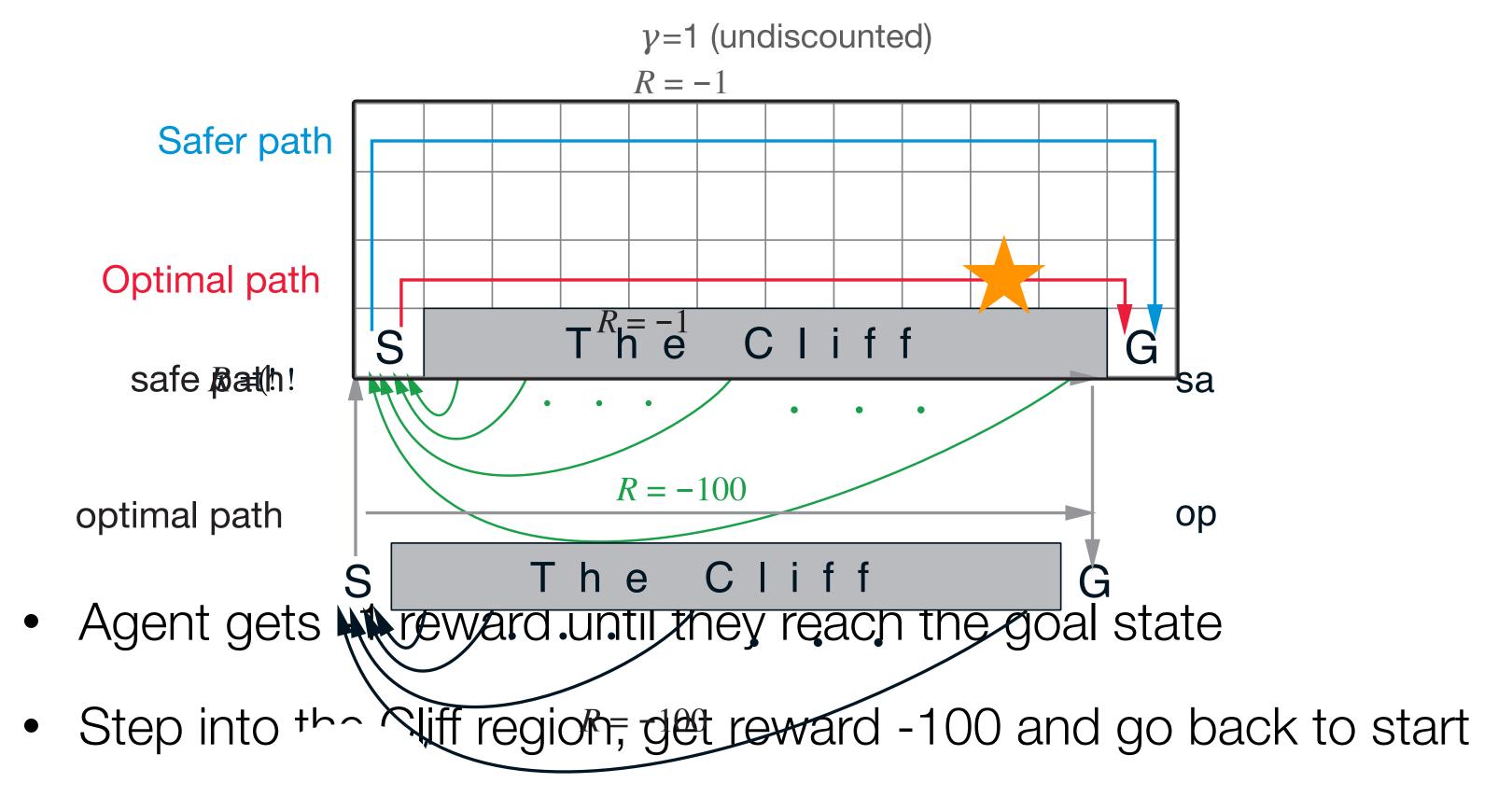
until S is terminal



Question: What information does this algorithm use?

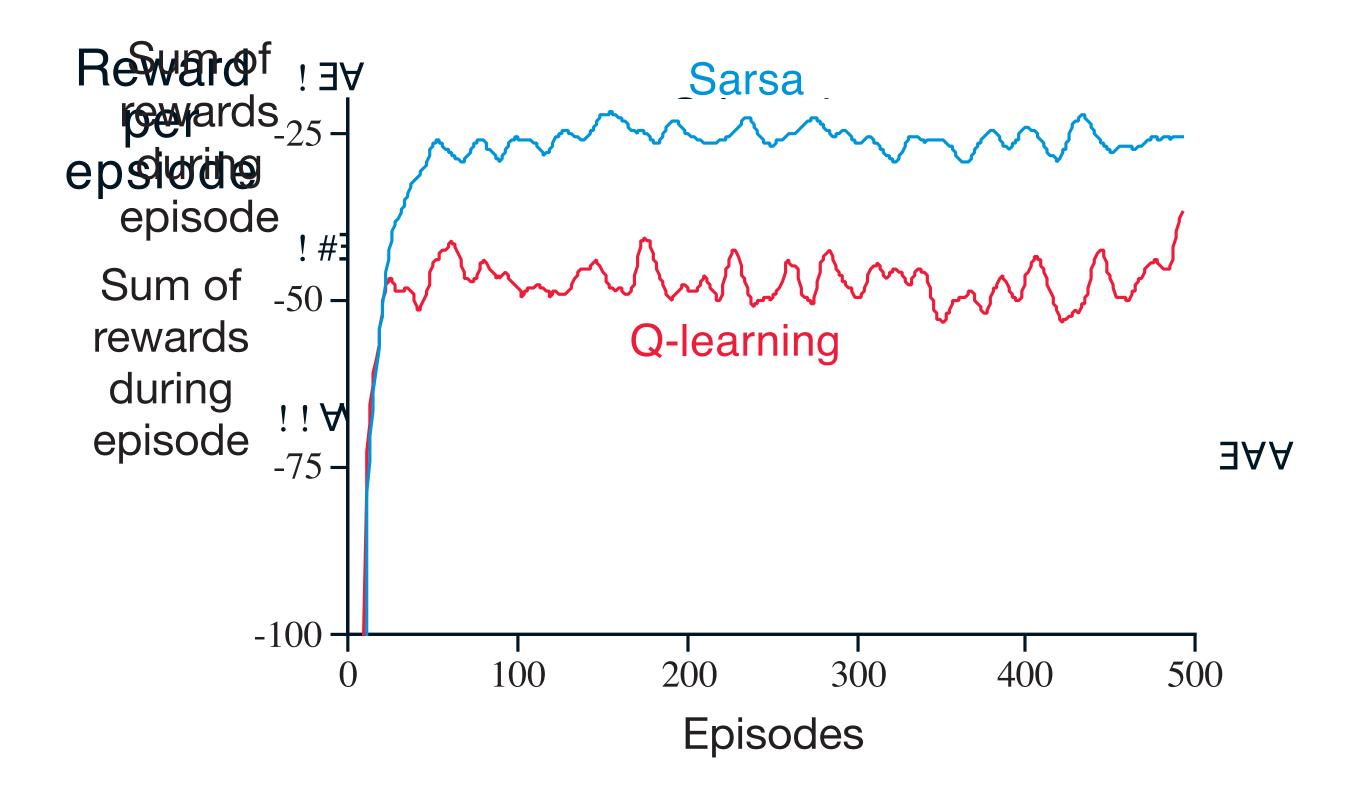
Question: Why aren't we estimating the policy π explicitly?

Example: The Cliff



- Question: How will Q-Learning estimate the value of this state?
- Question: How will Sarsa estimate the value of this state?

Performance on The Cliff



Q-Learning estimates optimal policy, but Sarsa consistently outperforms Q-Learning. (why?)

Summary

- Temporal Difference Learning bootstraps and learns from experience
 - Dynamic programming bootstraps, but doesn't learn from experience (requires full dynamics)
 - Monte Carlo learns from experience, but doesn't bootstrap
- Prediction: TD(0) algorithm
- Sarsa estimates action-values of actual ε -greedy policy
- Q-Learning estimates action-values of optimal policy while executing an ε-greedy policy